

3.7 The step response is obtained by accumulating the impulse response values.

$$s(n) = \sum_{k=-\infty}^n h(k) = \sum_{k=0}^n (0.8)^k - \sum_{k=0}^n (0.6)^k = \frac{1 - (0.8)^{n+1}}{1 - 0.8} - \frac{1 - (0.6)^{n+1}}{1 - 0.6}$$

Note that $s(n) \rightarrow H(1)$ as $n \rightarrow \infty$. Proof.

$$s(n) = \sum_{k=-\infty}^n h(k) \stackrel{\text{AE}}{\rightarrow} \sum_{k=-\infty}^{\infty} h(k) z^{-k} = H(1) \text{ for } z = 1$$

In this case we have $s(n) \rightarrow \frac{1}{1 - 0.8} - \frac{1}{1 - 0.6} = 2.5$ and

$$H(1) = \frac{0.2}{(1 - 0.8)(1 - 0.6)} = \frac{0.2}{0.2 \cdot 0.4} = 2.5$$