

5.11 The input is assumed to be scaled. The first critical node is after the first adder. The impulse response to this node is

$$0.4, -0.4, 0, \dots \Rightarrow S = 0.8$$

$\Rightarrow$  Increase the coefficients by a factor  $1/S$  to 0.5 and  $-0.5$ , respectively. The impulse response to the output node is (with the two first coefficients scaled):

$$(0.5 \cdot 0.75), (0.5(-0.75)) + (-0.5)0.75, (-0.5)(-0.75), 0, 0, \dots =$$

$$= 0.375, -0.75, 0.375, 0, 0 \Rightarrow S = 1.5$$

$\Rightarrow$  Decrease the coefficients by multiplying with a factor  $1/S$ . We obtain the new values 0.5 and  $-0.5$ , respectively. The new scaled impulse response becomes

$$(0.5 \cdot 0.5), (0.5(-0.5)) + (-0.5)0.5, (-0.5)(-0.5), 0, \dots =$$

$$= 0.25, -0.5, 0.25, 0, \dots$$

Using  $L_\infty$ -norm scaling we get the transfer function to the first critical noise node:  $H(z) = 0.4(1 - z^{-1})$ . The maximal value of the magnitude function is gotten for  $z = -1$ . Hence,  $|H|_{max} = 0.8$ . Thus, increase the first two coefficients to 0.5. The transfer function to the output node is

$$H(z) = 0.5(1 - z^{-1}) 0.75(1 - z^{-1})$$

The maximal value of the magnitude function is occur for  $z = -1$ . Hence,  $|H|_{max} = 1.5$ . Thus, decrease the last two coefficients to 0.5. In this case, the two scaling criteria leads to the same coefficients.