

# Exercise 1 in Robust Multivariable Control

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February 14, 2024

## 1 Introduction

This exercise contains four examples from the COMPl<sub>e</sub>ib's benchmarks [1].  
The models are available at

<https://users.isy.liu.se/rt/andersh/teaching/example5.m>

## 2 Exercise

Try to find a controller for each plant that achieves the best  $H_\infty$  norm,  $\gamma$ .  
Answer the following questions for each problem.

- (i) What is the best performance,  $\gamma$ .
- (ii) What is limiting in performance? Which condition comes into play?
- (iii) What happens with the controller when get close to the optimal  $\gamma$ ?

Table 1: Examples

| Case | $n$ | nmeas | ncon | $r$ | $\gamma$ |
|------|-----|-------|------|-----|----------|
| AC3  | 5   | 4     | 2    |     |          |
| AC9  | 10  | 5     | 4    |     |          |
| TF1  | 7   | 4     | 2    |     |          |
| NN16 | 8   | 4     | 4    |     |          |

- (iv) Try to reduce the order of the controller ( $r$ ). Is the controller sensitive to variations?
- (v) Is the design problem well formulated? What may be missing?

## References

- [1] F. Leibfritz. Compleib: Constraint matrix-optimization problem library – a collection of test examples for nonlinear semidefinite programs, control system design and related problems. Technical report, Department of Mathematics, University of Trier, Trier, Germany, 2004.